Queueing Systems

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QUEUEING SYSTEMS General

• Queueing systems constitute a central tool in modelling and performance analysis of e.g. telecommunication systems and computer systems.

• Describes contention on the resources

– in queueing systems the resources are called servers

– in applications, the resources may be trunks, capacity . . .

• The “customers” arriving at a queue may be calls, messages, packets, tasks . . .

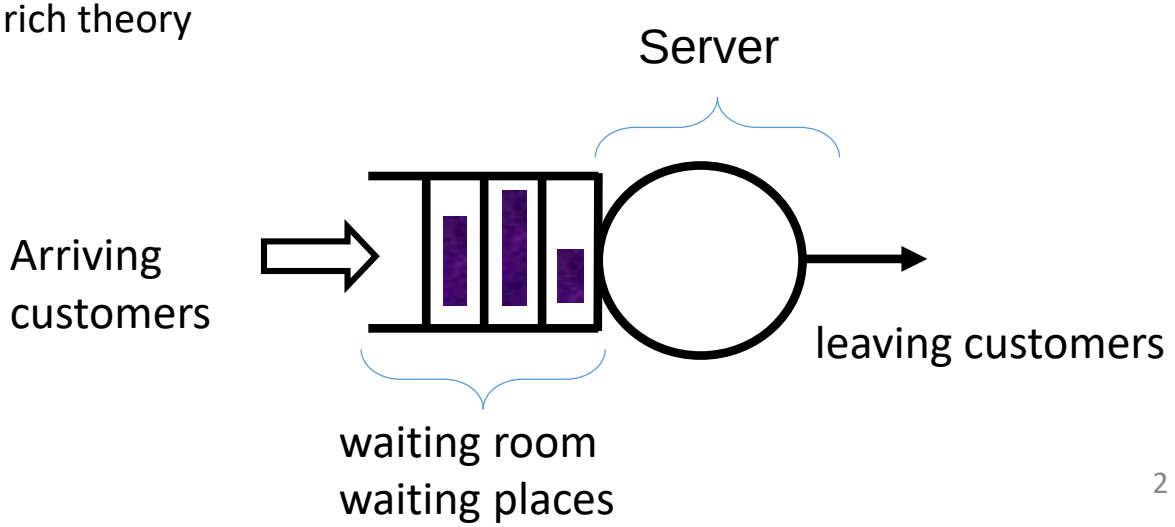
• Often the systems are complex (for instance communication network, operating system) and contains many queues, which form a network of queues, i.e. a queueing network.

– in the beginning we focus on systems consisting of a single queue

– there are many types of queues, giving rise to a rich theory

Example:

Single server queue



Differentiating factors in queueing systems

- Arrival process
  - interarrival times
  - group arrivals
- Service process
  - service times (requested service work)
- Number of servers
- Number of queues
- Number of waiting places
  - division of the waiting room between the queues
- Service discipline
  - FIFO, LIFO
  - shortest jobs first
  - most profitable jobs first
- Scheduling
  - round robin
  - processor sharing
  - priorities
- Information available
  - upon choice of a queue, does one know the lengths of queues, the service times of individual customers . . .
- Discrete time (slotted) / continuous time queues
- Other factors (in real life)
  - screening of the customers
  - bribing
  - . . .

The notation of queueing systems (Kendall)

- For a unique definition of queueing systems, the following notation is usually used: A/S/m/c/p, where

$\underbrace{A}$	/	$\underbrace{S}$	/	$\underbrace{m}$	/	$\underbrace{c}$	/	$\underbrace{p}$
arrival process		service process		number of servers		number of system places		size of customer population

- A and S are substituted by one of the commonly used symbols as the case may be.
- Usually the term queue length refers to the total number of customers in the system (including both waiting customers and those in service).
- The parameter c includes both waiting places and service places
  - may be omitted from the notation, whence by default its value is infinite
- The size of the customer population s also on optional parameter
  - may be omitted from the notation, whence by default its value is infinite

A (arrival process)

- Defines the type of arrival process
- Often it is thought that the interarrival times are independent (renewal process), whence the process is determined by the type of interarrival distribution.

Commonly used symbols are

M exponential interarrival distribution (M = Markovian, memoryless); Poisson process

D deterministic, constant interarrival times

G general (unspecified)

E_k Erlang-k distribution

PH phase distribution

Cox Cox distribution

- More abbreviations are introduced as needed.

S (service process)

- Defines the distribution of the customer's service time
- The service time is affected by two factors
  - – the required work requested by the customer (e.g. the size of a data packet to be sent, kB)
  - – the service rate of the server (e.g. kB/s) – the service time is the ratio of these
- In Kendall's notation, the type of the service time distribution is indicated by substituting an appropriate symbol for S; commonly the same symbols (M, D, G, etc.) are being used as for defining the type of the interarrival time distribution

Example 1. The queue M/M/1

- Poisson arrival process
- exponential service time distribution
- single server
- unlimited number of waiting places

Example 2. The queue M/M/m/m

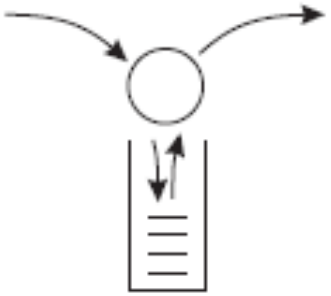
- Poisson arrival process
- exponential service time distribution
- m servers and m system places ⇒ no waiting room, so called loss system

Queueing discipline / scheduling

- Ordinary queue, service in the order of arrivals

FCFS First Come First Served

FIFO First In First Out



- Stack, the latest arrival is being served first

LIFS Last Come First Served

LIFO Last In First Out

- There are three sub-cases of a stack
  - pre-emptive resume

    the arriving customer pre-empts the ongoing service, which is then resumed when the interrupted customer is again taken into the server, continuing from the same point on as at the time of interruption

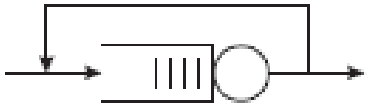
  - pre-emptive restart

    the arriving customer pre-empts the ongoing service; the service is started from the beginning when the interrupted customer is again taken into the server

  - non-pre-emptive

    the arriving customer waits until the ongoing service is finished before being taken into the server

Queueing discipline / scheduling (continued)

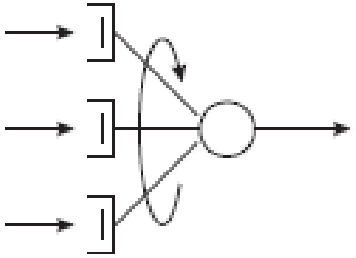


- Service in rotating order

RR Round robin

– each customer receives, in turn, a small “time slice” of service

– polling



- Sharing the capacity of the server

PS Processor sharing

– all customers in the queue are receive service simultaneously

– the capacity is shared evenly between the customers (the service rate received by each customer is inversely proportional to the number of customers in the queue)

– an idealized form of RR (the time slices tend to zero)

Other service disciplines are e.g.

- SIRO (Service In Random Order)
- SSF (Shortest Jobs First): the service time has to be known in advance; this minimizes the mean waiting time

Queueing discipline / scheduling (continued)

- A queueing discipline is called work conserving, if the capacity of the server / servers is not wasted, i.e. no server is idle if there is at least waiting customer in the system.

- Not all disciplines are work conserving, e.g.
  - LCFS / pre-emptive restart
  - systems, where the server can take a “vacation”